

Estimation of the characteristic chemical time scale in a flame by the PIV



Chernov A.A., Shmakov A.G., Korobeinichev O.P.

*Voevodsky Institute of Chemical Kinetics and Combustion SB RAS, Institutskaya 3, 630090, Novosibirsk, Russia

**Siberian State University of Geosystems and Technologies 630032, Novosibirsk, Russia

Deceleration of Darrieus-Landau instability.

the Markstein mechanism hydrodynamic stability Darrieus-Landau instability

$$\mathbb{K} = \frac{1}{A} \frac{dA}{dt} = \nabla(\vec{n} \times (\vec{v}_s \times \vec{n})) + (\vec{U} \cdot \nabla)(\vec{n} \cdot \vec{v})$$

Zeldovich - Barrenblatt hypotheses (result the Euler equation calculation)

The gas flow near the flame front on both sides of the front obeys the Euler equation and the continuity equation

$$\frac{\partial \vec{U}}{\partial t} + (\vec{U} \cdot \nabla) \vec{U} = -\frac{1}{\rho} \nabla p \quad \text{div} \vec{U} = 0 \quad U_f = \frac{\int_{-\infty}^{+\infty} \dot{\omega}(\vec{n} \cdot d\vec{x})}{\rho Y_R} \quad \dot{\omega} = \rho Y_R^n Y_{O_2}^m A T^b \exp\left(-\frac{E}{RT}\right)$$

Looking for the perturbation increment: $\omega (\sigma = \rho_0 / \rho_{burn})$

Landau (1944): $U_f = U_0 \quad l_f = 0 \quad P'_0 - P'_{burn} = 0$

$$\left(\frac{\omega}{\sigma k u_0}\right)^2 + \frac{2}{1+\sigma} \frac{\omega}{\sigma k u_0} + \frac{1-\sigma}{\sigma(1+\sigma)} = 0 \quad \omega = -\frac{\sigma k u_0}{\sigma+1} \left(1 \pm \sqrt{\frac{\sigma^2 + \sigma - 1}{\sigma}}\right) \neq 0$$

Zeldovich - Barrenblatt result the Euler equation calculation (1960)

$$P'_0 - P'_{burn} \neq 0 \quad P'_0 - P'_{burn} = -2\rho_1(u_0)^2(\sigma-1)\mu \frac{\partial^2 x_f}{\partial y^2}$$

$$l_f = X/U_0 \quad U_f = U_0 \left(1 + \frac{L_m}{R_f}\right) \quad Ze = \frac{E(T_{max} - T_0)}{RT_{max}^2}$$

$$\omega = -\frac{\sigma k u_0}{\sigma+1} \left(1 + L_m k \pm \sqrt{\frac{\sigma^2 + \sigma - 1}{\sigma} + L_m k(L_m k - 2\sigma)}\right) = 0$$

$$L_m = \left[l_f \frac{D}{\chi}\right]_{\text{Thdiff}} + \left[l_f \frac{(X-D)Ze}{\chi}\right]_{\text{ThChem}}$$

$$L_m = \left[l_f \frac{D}{\chi}\right] = l_f \leftarrow Le_s = \frac{D}{\chi} = 1$$

$$\tau_{chem} = \tau_{chM} = \frac{L_m}{U_0}$$

Ya B. Zeldovich, G. I. Barrenblatt, V. B. Librovich, G. M. Makhviladze, The Mathematical Theory of Combustion and Explosions. Consult. Bureau, 1985
F. Cresta, M. Matalon, Strain rate effects on the nonlinear development of hydrodynamically unstable flames, Proceedings of the Combustion Institute Volume 33, Issue 1, 2011, Pages 1087-1094

Experimental visualization of the combustion wave . Method PIV.

Normal burning velocity of the Fuel/air flame was determined by extrapolating the dependence of the local burning velocity on the local curvature of the flame front to the zero curvature

two pulsed Nd:YAG lasers
pulse duration 5 ns
CCD camera 1360x1024
Pixel size ~9x9 μm

Mache-Hebra burner

flame wave

3D

2D

$U_f = \frac{\int_{-\infty}^{+\infty} \dot{\omega}(\vec{n} \cdot d\vec{x})}{\rho Y_R}$

Dependence of local U_f on the radius of curvature R_f

--- Linear theory Zeldovich, Clavin, Matalon...
— Non-linear theory Law, Sung....

$$U_f = U_0 \left(1 + \frac{L_{CCML}}{R_f}\right)$$

$$U_f = \frac{U_0}{\left(1 - \frac{L_{CCML}}{R_f}\right)} = U_0 \left(1 + \frac{L_{CCML}}{R_f}\right) \left(\frac{1}{1 - \left(\frac{L_{CCML}}{R_f}\right)^2}\right)$$

Gas stream tubes. To determine the geometric parameters of stream tubes, the experimental data were processed as follows. The discrete points obtained experimentally by PIV were used to construct a two-dimensional velocity field by cubic spline interpolation:

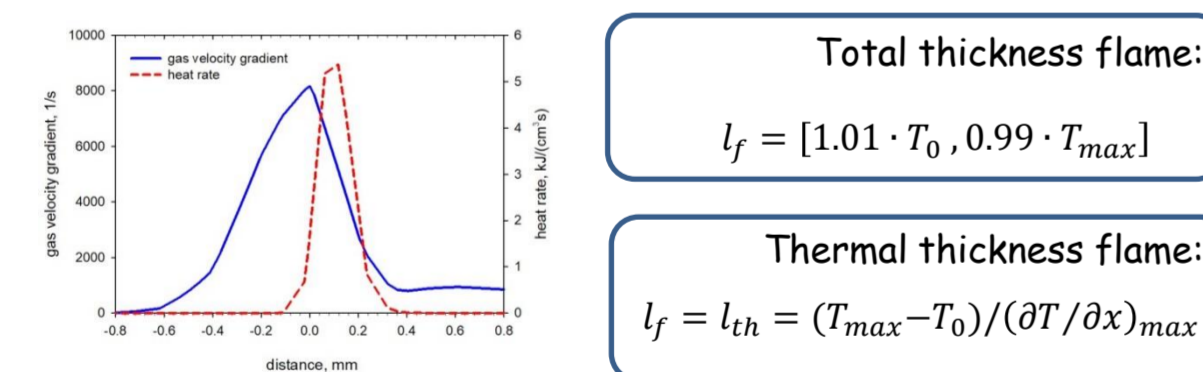
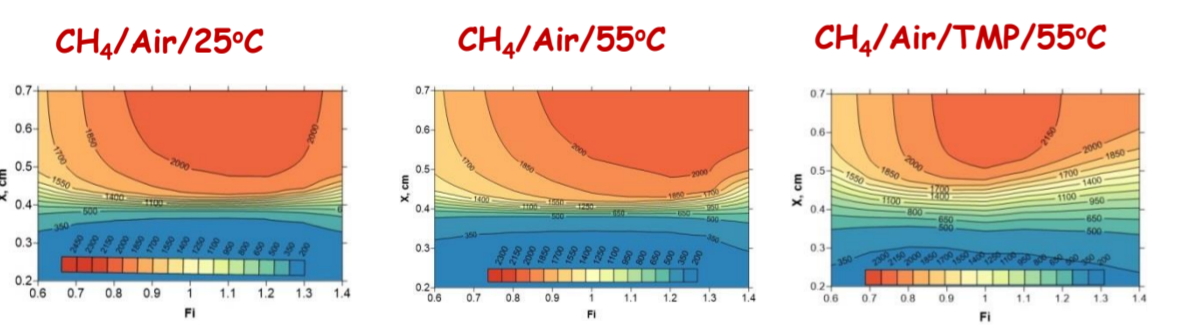
$$\{V_x, V_y, (X, Y)\} \rightarrow V_x(x, y), V_y(x, y)$$

Streamlines are obtained by numerically integrating the equations:

$$\frac{\partial y}{\partial x} = \frac{v_y(x, y)}{v_x(x, y)} \mid y(x = x_0) = y_0$$

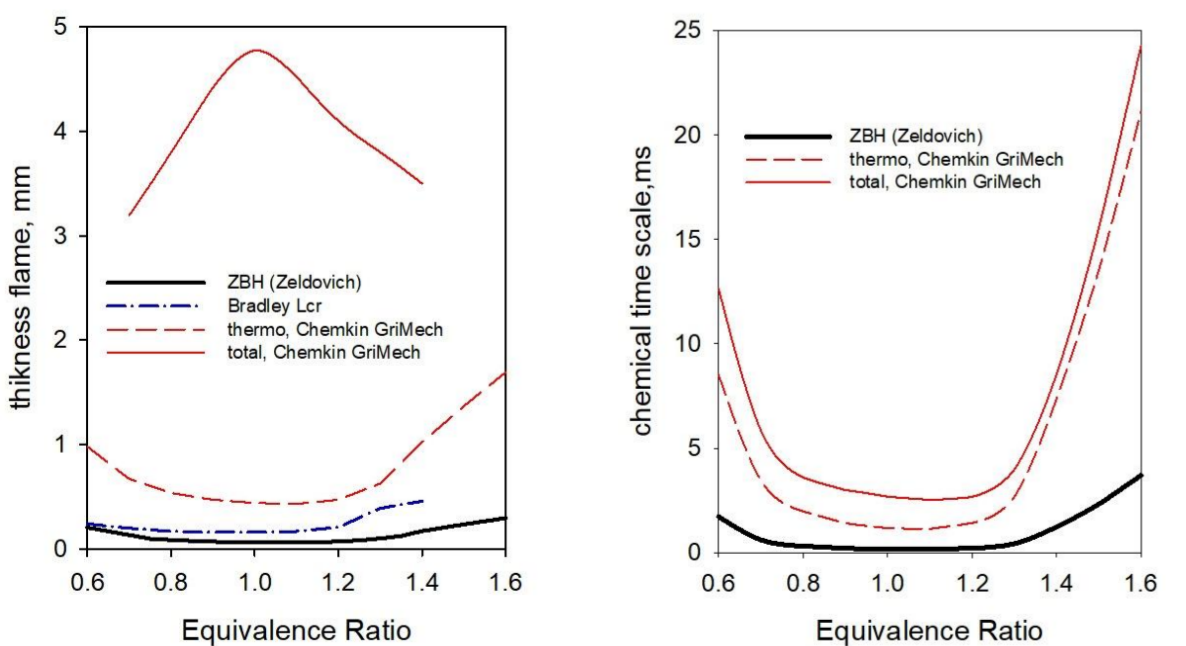
1D-CHEMKIN model flame thickness

Temperature dependence on X and equivalence ratio



ZBH thickness flame and chemical time scale (Zeldovich et al.):

$$l_f = X/U_0, [mm] \quad \tau_{chem} = \frac{(X/U_0)}{U_0}, [s]$$



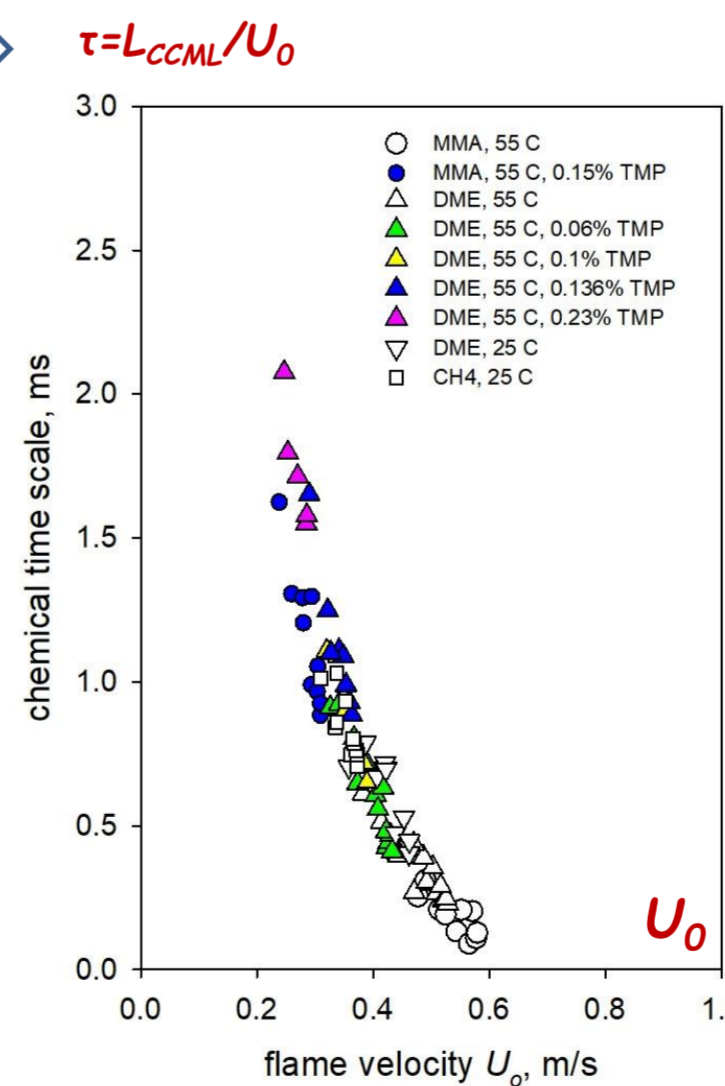
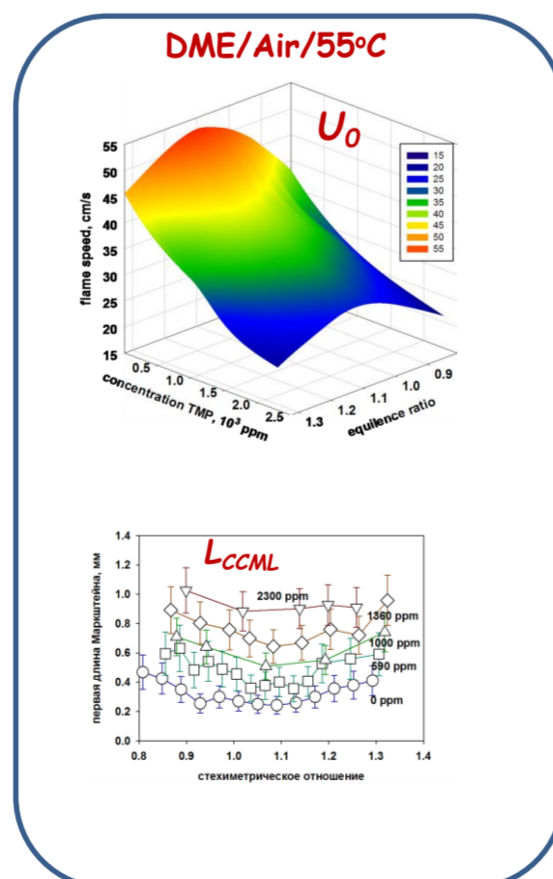
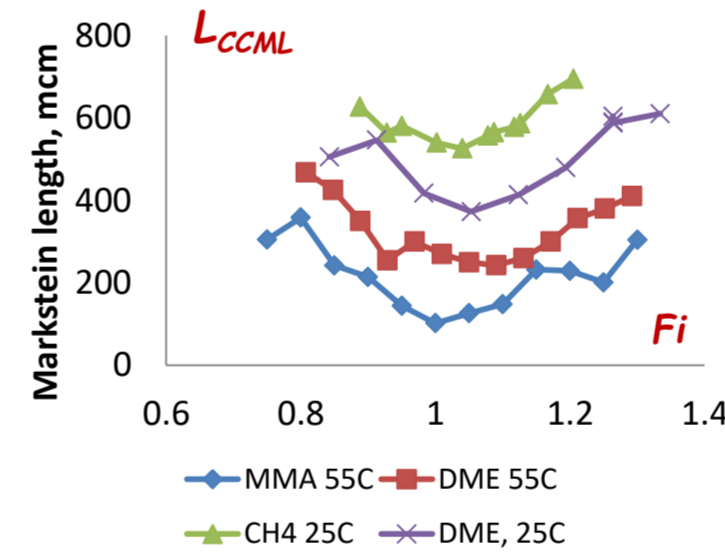
Experimental results

Experimental result measurements consumption curvature Markstein - Zeldovich - Barrenblatt length L_{CCML} and chemical time scale $\tau = L_{CCML}/U_0$

Fuel:
CH4 - methane
DME - dimethyl ether
MMA - methyl methacrylate

Inhibitor:
TMP - trimethyl phosphate

Experiment conditions:
Fuel/Air flame
P=1 atm
t=25 and 55 °C



Industrial combustion

Zimont correlation has been used for many engineering problems for 20 years and is used by default in the ANSYS Fluent software

The turbulent combustion velocity, U_T - function of the physico-chemical properties of combustible mixture and turbulence parameters:

$$\frac{\partial}{\partial t}(\rho c) + \nabla \cdot (\rho \vec{v} c) = \nabla \cdot \left(\frac{\mu_T}{Sc_T} \nabla c\right) + \rho S_{chem}$$

$$\rho S_{chem} = \rho_0 U_T \nabla(1 - [Fuel]/[Fuel_0])$$

Zimont correlation, (1979, 2000): $U_T \approx u_{RMS} \times \left(\frac{\tau_{turb}}{\tau_{chem}}\right)^{1/4}$

u_{RMS} - RMS (root-mean-square) velocity
 τ_{turb} - turbulence time scale (s)
 τ_{chem} - chemical time scale (s)

